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Unit 5, Lesson 9

Multiplying Rational Numbers

Let's multiply signed numbers.

9.1 Before and After

Where was the girl

1. 5 seconds *after* this picture was taken? Mark her approximate location on the picture.
2. 5 seconds *before* this picture was taken? Mark her approximate location on the picture.



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9.2 Backwards in Time

A traffic safety engineer was studying travel patterns along a highway. She set up a camera and recorded the speed and direction of cars and trucks that passed by the camera. Positions to the east of the camera are positive, and to the west are negative.

1. Here are some positions and times for one car:

position (feet)	-180	-120	-60	0	60	120
time (seconds)	-3	-2	-1	0	1	2

- a. In what direction is this car traveling?
- b. What is its velocity?
2. a. What does it mean when the time is zero?
- b. What could it mean to have a negative time?

3. Here are the positions and times for a different car whose velocity is -50 feet per second:

position (feet)				0	-50	-100
time (seconds)	-3	-2	-1	0	1	2



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a. Complete the table with the rest of the positions.

b. In what direction is this car traveling? Explain how you know.

4. Complete the table for several different cars passing the camera.

	velocity (meters per second)	time after passing camera (seconds)	ending position (meters)	equation
car C	+25	+10	+250	$25 \cdot 10 = 250$
car D	-20	+30		
car E	+32	-40		
car F	-35	-20		
car G	-15	-8		

5. a. If a car is traveling east when it passes the camera, will its position be positive or negative 60 seconds *before* it passes the camera?

b. If we multiply a positive number and a negative number, is the result positive or negative?



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6. a. If a car is traveling west when it passes the camera, will its position be positive or negative 60 seconds *before* it passes the camera?
- b. If we multiply two negative numbers, is the result positive or negative?

9.3 Cruising

Interactive digital version available

a.openup.org/ms-math/en/s/ccss-7-5-9-3



Around noon, a car was traveling -32 meters per second down a highway. At exactly noon (when time was 0), the position of the car was 0 meters.

1. Complete the table.

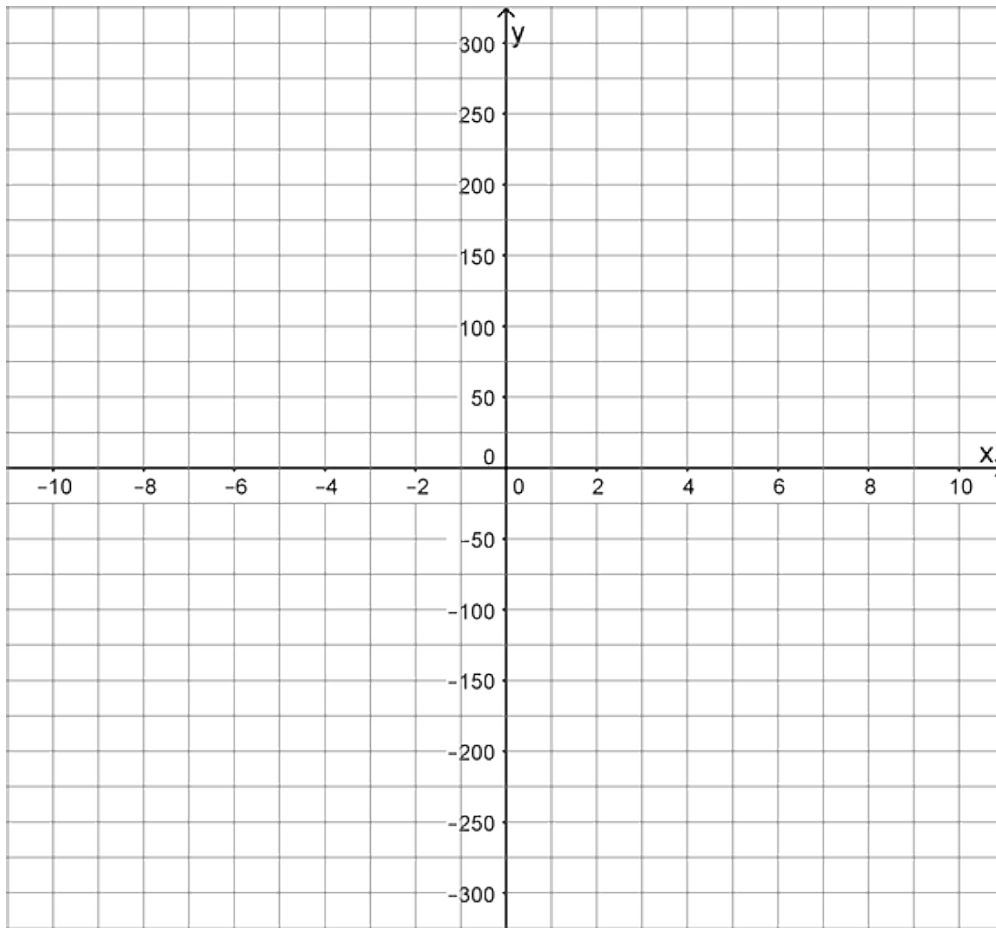
time (s)	-10	-7	-4	-1	2	5	8	11
position (m)								

2. Graph the relationship between the time and the car's position.

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3. What was the position of the car at -3 seconds?

4. What was the position of the car at 6.5 seconds?

➡ Are you ready for more?

Find the value of these expressions without using a calculator.

$(-1)^2$

$(-1)^3$

$(-1)^4$

$(-1)^{99}$

9.4 Rational Numbers Multiplication

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Grid

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a.openup.org/ms-math/en/s/ccss-7-5-9-4



1. Fill in the shaded boxes in the multiplication square below

5						0	5	10	15	20	
4						0	4	8	12	16	
3						0	3	6	9	12	
2					-2	0	2	4	6	8	
1						0	1	2	3	4	
0						0	0	0	0	0	
-1											
-2											
-3											
-4											
-5											
	-5	-4	-3	-2	-1	0	1	2	3	4	5

2. Look at the patterns along the rows and columns. Continue those patterns into the unshaded boxes.

3. Complete the whole table.



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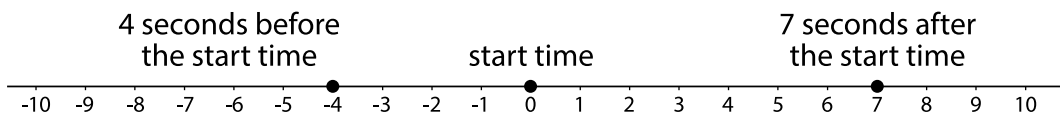
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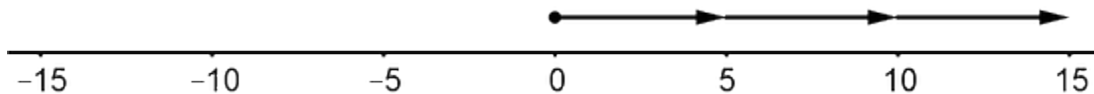
4. What does this tell you about multiplication with negative numbers?

Lesson 9 Summary

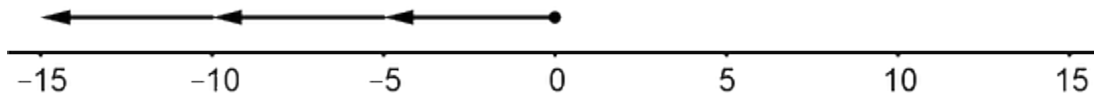
We can use signed numbers to represent time relative to a chosen point in time. We can think of this as starting a stopwatch. The positive times are after the watch starts, and negative times are times before the watch starts.



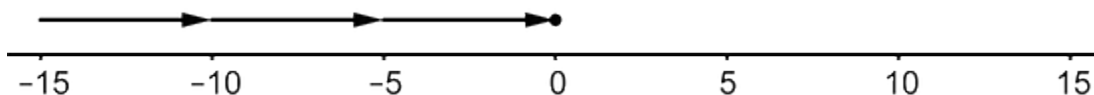
If a car is at position 0 and is moving in a positive direction, then for times after that (positive times), it will have a positive position. A positive times a positive is positive.



If a car is at position 0 and is moving in a negative direction, then for times after that (positive times), it will have a negative position. A negative times a positive is negative.



If a car is at position 0 and is moving in a positive direction, then for times *before* that (negative times), it must have had a negative position. A positive times a negative is negative.



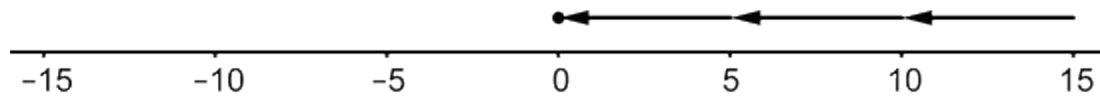
If a car is at position 0 and is moving in a negative direction, then for times *before* that (negative times), it must have had a positive position. A negative times a negative is positive.



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Here is another way of seeing this:

We can think of $3 \cdot 5$ as $5 + 5 + 5$, which has a value of 15.

We can think of $3 \cdot (-5)$ as $(-5) + (-5) + (-5)$, which has a value of -15.

We can multiply positive numbers in any order:

$$3 \cdot 5 = 5 \cdot 3$$

If we can multiply signed numbers in any order, then $-5 \cdot 3 = -15$.

We can find $-5 \cdot (3 + (-3))$ two ways:

- $-5 \cdot 0 = 0$
- $-5 \cdot 3 + (-5) \cdot (-3)$ (this is the distributive property)

That means that

$$-5 \cdot 3 + (-5) \cdot (-3) = 0$$

Which is the same as

$$-15 + (-5) \cdot (-3) = 0$$

So

$$-5 \cdot (-3) = 15$$

There was nothing special about these particular numbers. This always works!

- A positive times a positive is always positive
- A negative times a positive or a positive times a negative is always negative
- A negative times a negative is always positive